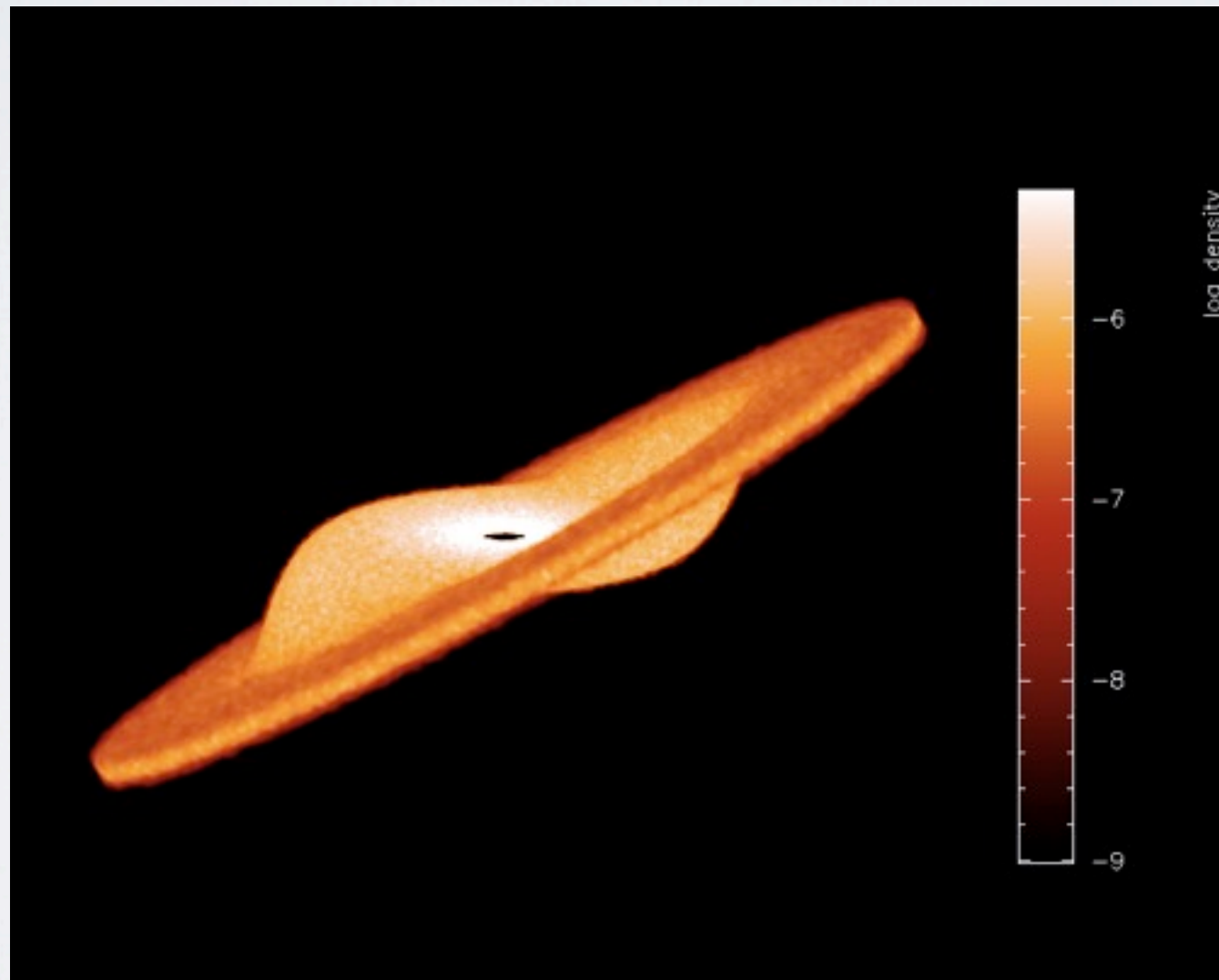


Resonant stars / disk interactions: implications for MBH evolution

Michal Bregman & Tal Alexander

Weizmann Institute of Science



Simulation of a warped accretion disk- G.Lodato

The key question

Motivation:

- Spin affects accretion efficiency.
- The puzzle of very massive BH in the early universe.
- Evidence for MBH spin precession.
- Warped disks (NGC4258)

RR mechanism

Perturbing stars

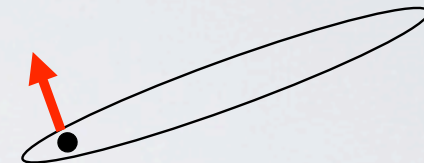
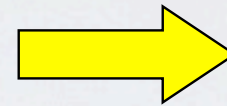
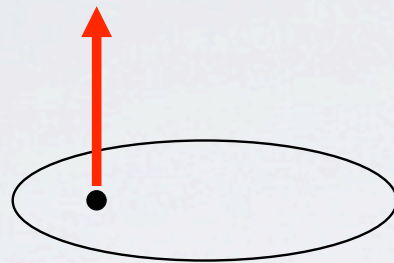


Stationary ellipses
in point mass potential

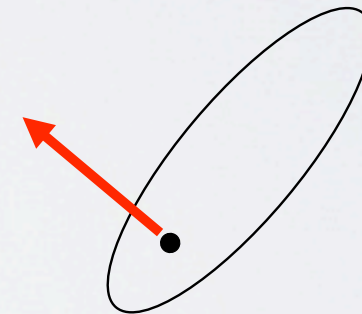
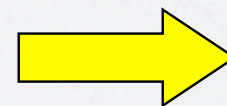
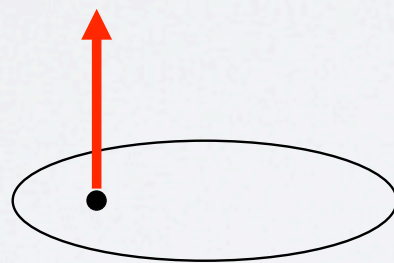


Planar rosettes in
spherical potential

Effect on perturbed star



Scalar resonant relaxation



Vector resonant relaxation

Rauch & Tremaine 96

vector RR

The residual torque on a test mass $\tau = N_{\star}^{1/2} \frac{GM_{\star}}{r}$

The coherence time $t_0 = A_0 L_c / \tau = A_0 P M_{\bullet} / (M_{\star} N_{\star}^{1/2})$

$$t \gg t_0 \quad |\Delta L|/L_c = 1 \quad \rightarrow \quad [(\Delta L)_{t_0}/L_c](t_{vRR}/t_0)^{1/2} = 1$$

$$t_{vRR} = \frac{1}{\beta_{\nu}^2} \frac{M_{\bullet}}{M_{\star}} \frac{P}{N_{\star}^{1/2}} \left(\frac{r}{R}\right)^{2\theta}$$

$$M_{\star} N_{\star} \ll M_{\bullet}$$
$$\theta = \text{sgn}(r - R)$$

Disc viscosity

In plane viscosity-

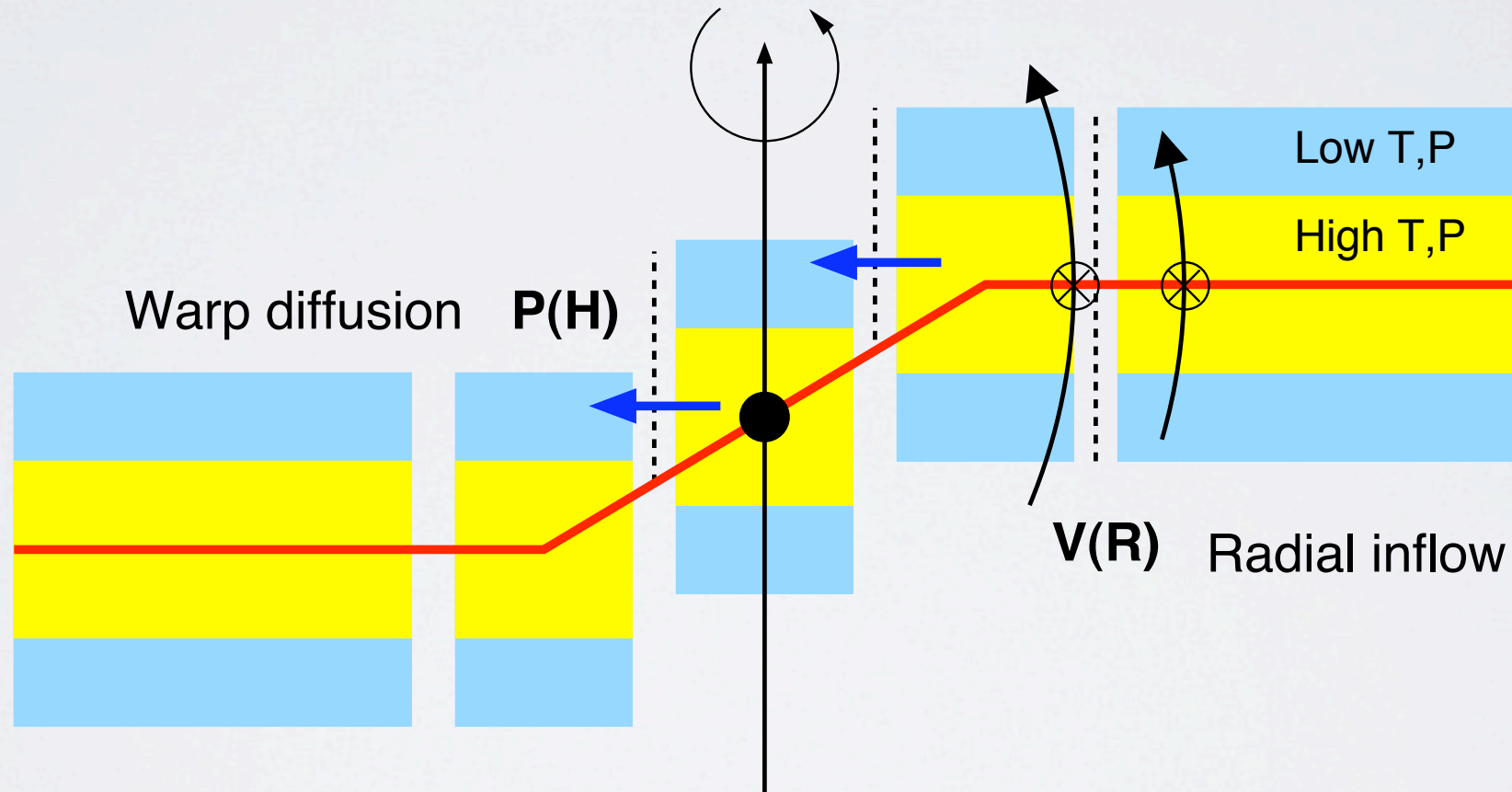
$$\nu_1 = \alpha_1 C_s H$$



$$\alpha_2 = \frac{1}{2\alpha_1}$$

Perpendicular viscosity-

$$\nu_2 = \alpha_2 C_s H$$



α disk model: stress tensor $\sigma_{ij} = \alpha P$ $(0 < \alpha < 1)$

$$t_{visc} = R^2 / \nu$$

RR warping of an accretion disk

Angular momentum condition

$$\overset{L_{disk}}{w M_d(R) L_c(R)} \leq \overset{L_{\star}}{N_{\star}^{1/2} M_{\star} L_c(r)} \quad r_L \leq r$$

Timescale condition

$$w t_{vRR}(r, R) \leq t_{visc} \quad t_{visc} = \min(t_{\nu_1}, t_{\nu_2})$$

$$r_t^{(-)} \leq r \leq r_t^{(+)}$$

The disk will warp only if $\max(r_t^{(-)}, r_L) \leq r \leq r_t^{(+)}$

where: r radius in the cusp, R radius in the disk, $L_c = (GM_{\bullet} r)^{1/2}$ and $w^2 = 2(1 - \cos\omega)$

RR disk warping and early MBH evolution

RR may affect low-mass MBHs in early universe:

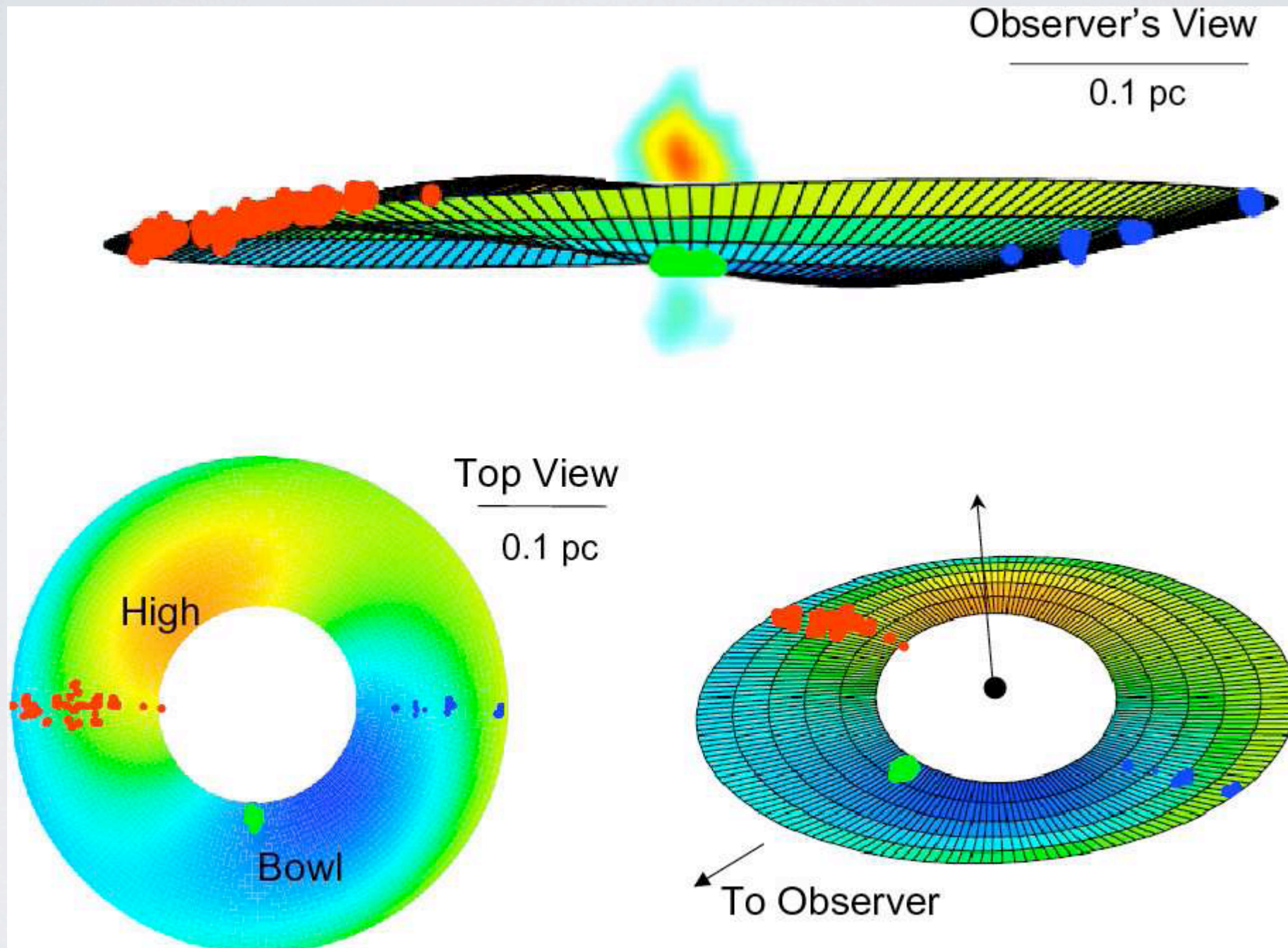
$$\frac{\sqrt{N}}{Q} P \sim T_{vRR} < t_{inflow} \sim \frac{(R/H)^2}{\alpha} P$$

$$Q \lesssim 10^5 - 10^6$$

$$Q = M_{\bullet}/M_{\star}$$

Maser disk NGC4258

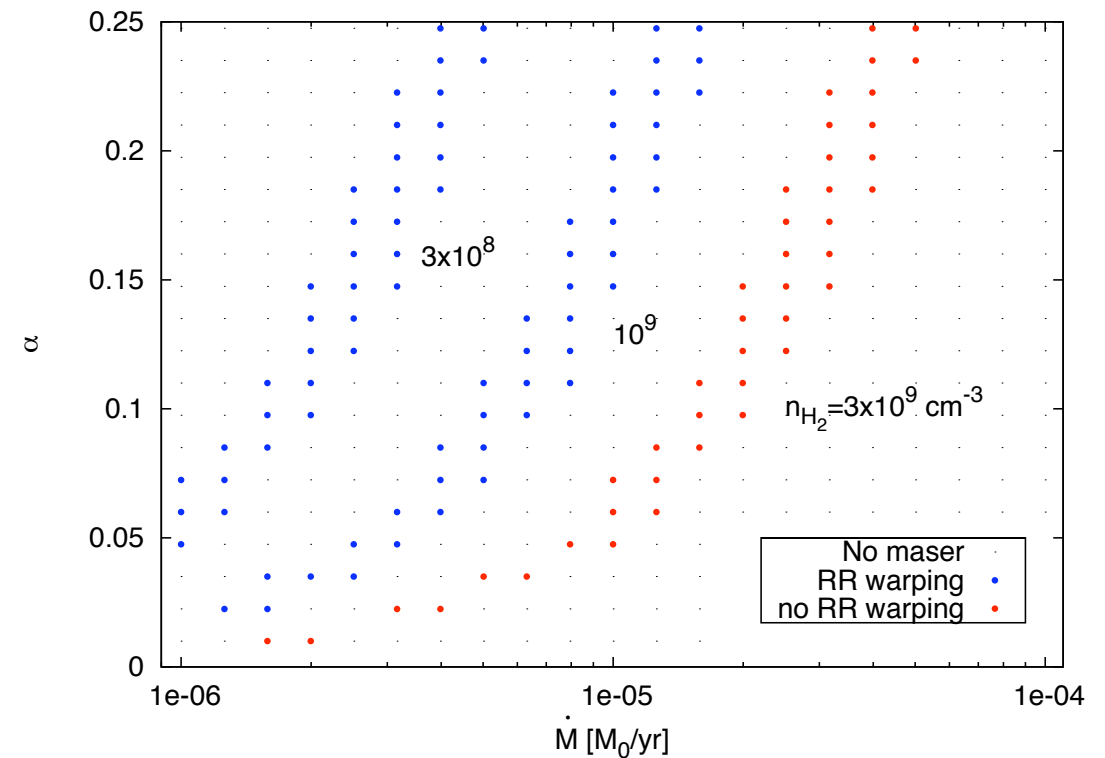
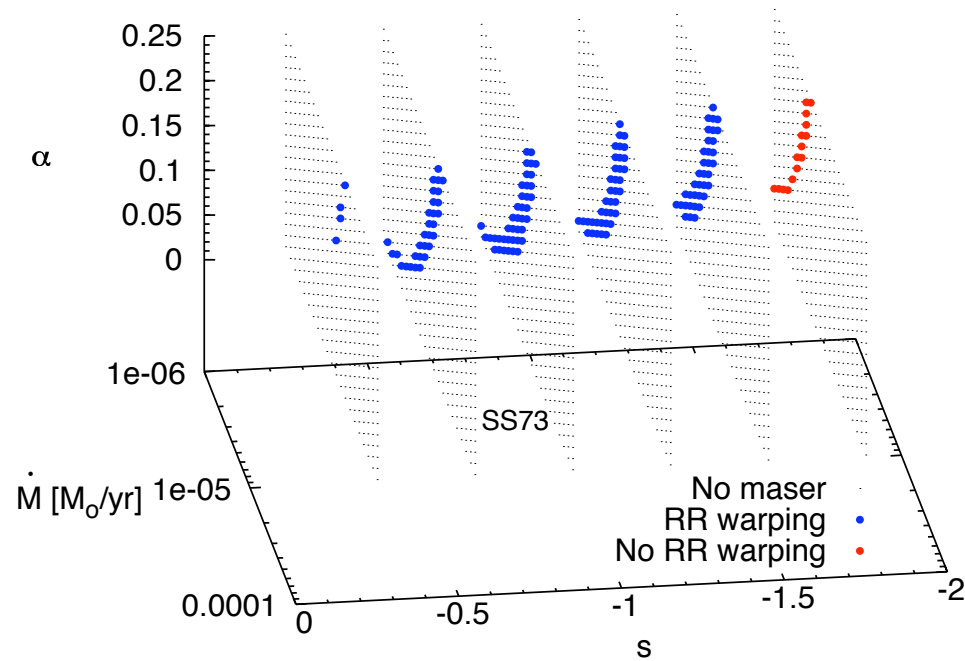
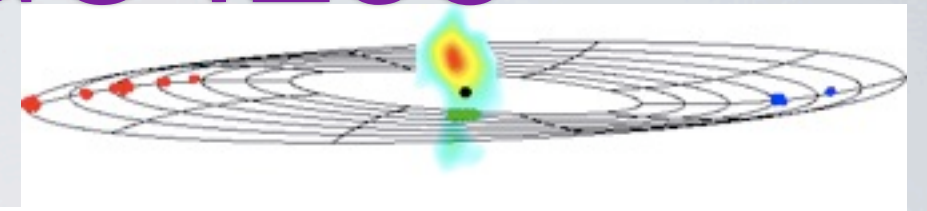
Herrnstein et al 1996



Radio measurements of x , v , \dot{v}

$$D = 7.2 \pm 0.3 \text{ Mpc} \quad M_{\bullet} = 3.7 \times 10^7 M_{\odot} \quad R = 0.14 - 0.28 \text{ pc} \quad \gamma = 1.5 \quad \text{warp} \sim 8^{\circ}$$

RR disk warping of NGC4258



$$s = -3/4$$

Bregman et.al 2009 ApJ

The $O(10_{\pm})$ NGC4258 disk warp on the $O(0.1 \text{ pc})$ scale is naturally explained by RR torques of $O(10^6)$ stars on the $O(1 \text{ pc})$ scale.

Preliminary work and future steps

Warp diffusion in accretion discs

mass conservation + angular momentum conservation

$$\frac{\partial \mathbf{L}}{\partial t} = \frac{3}{R} \frac{\partial}{\partial R} \left[\frac{R}{L} \frac{\partial}{\partial R} (\nu_1 L) \mathbf{L} \right] + \frac{1}{R} \frac{\partial}{\partial R} \left[\frac{1}{2} \nu_2 R L \frac{\partial(\mathbf{L}/L)}{\partial R} \right]$$

diffusive part

$$+ \frac{1}{R} \frac{\partial}{\partial R} \left[(\nu_2 R^2 \frac{\partial(\mathbf{L}/L)}{\partial R} - \frac{3}{2} \nu_1) \mathbf{L} \right] + \dot{\mathbf{L}}_{(+)} + \dot{\mathbf{L}}_{(-)} + \mathbf{T}_{RR}$$

advective part

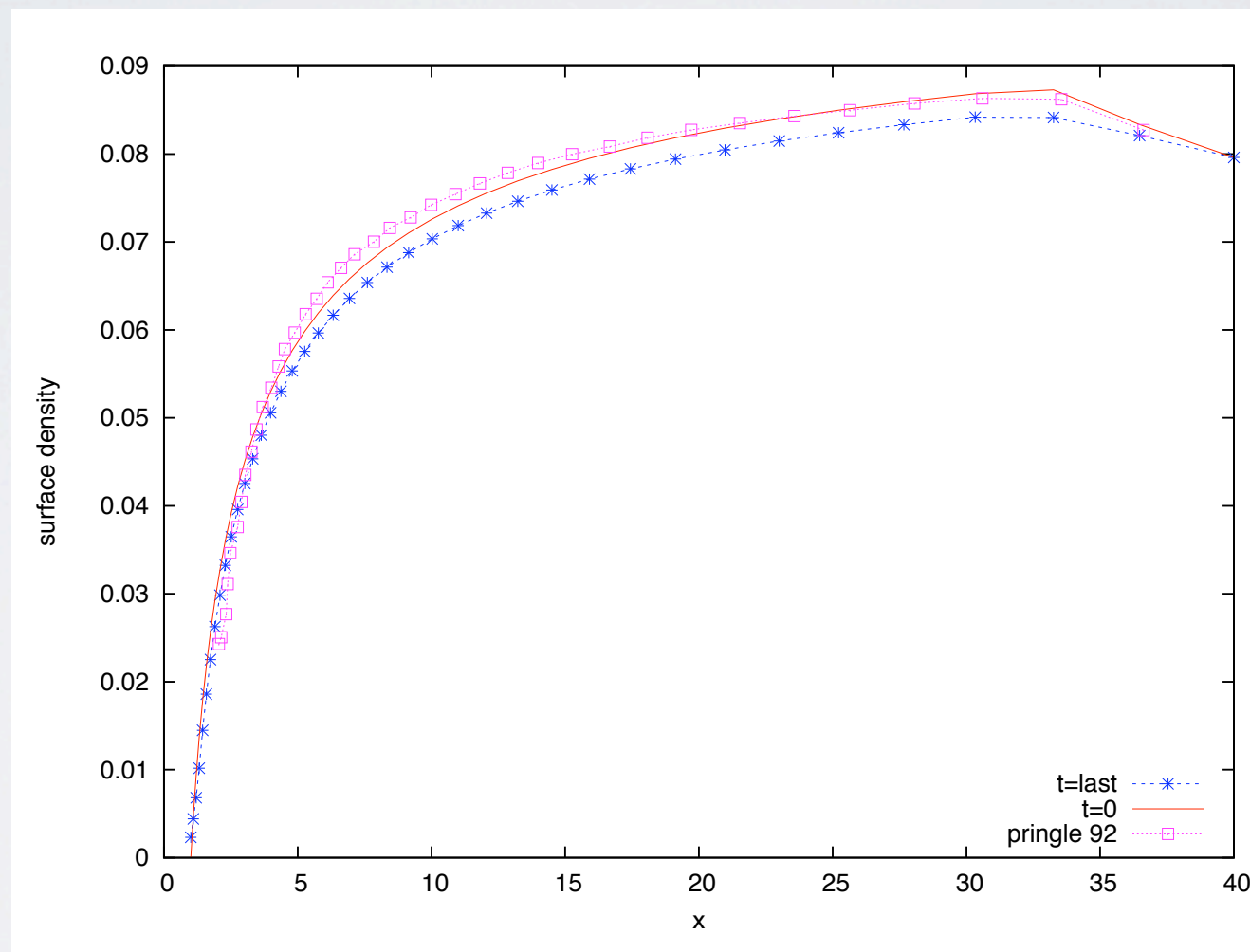


source term

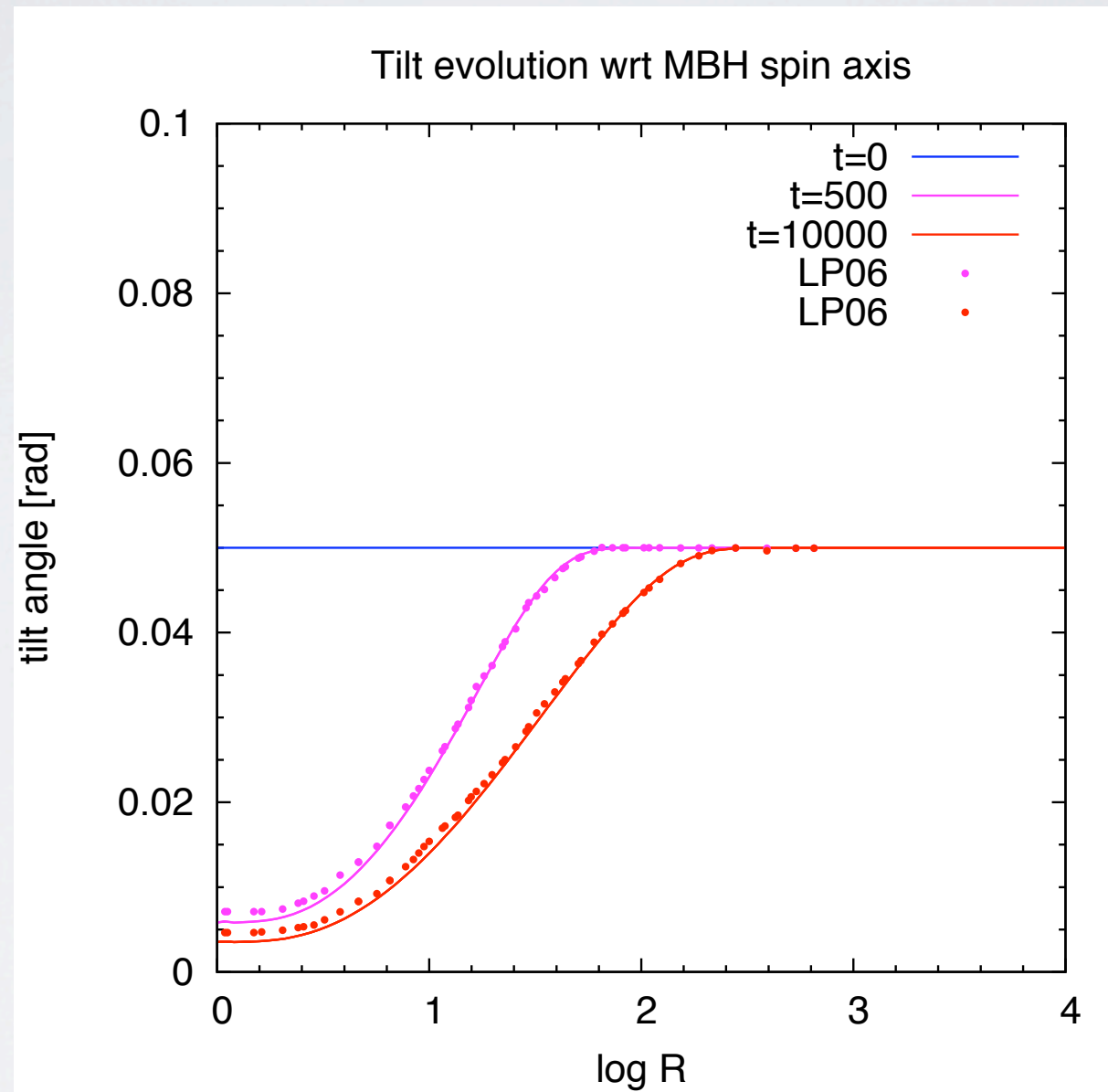


sink term

Surface density distribution for steady state disk



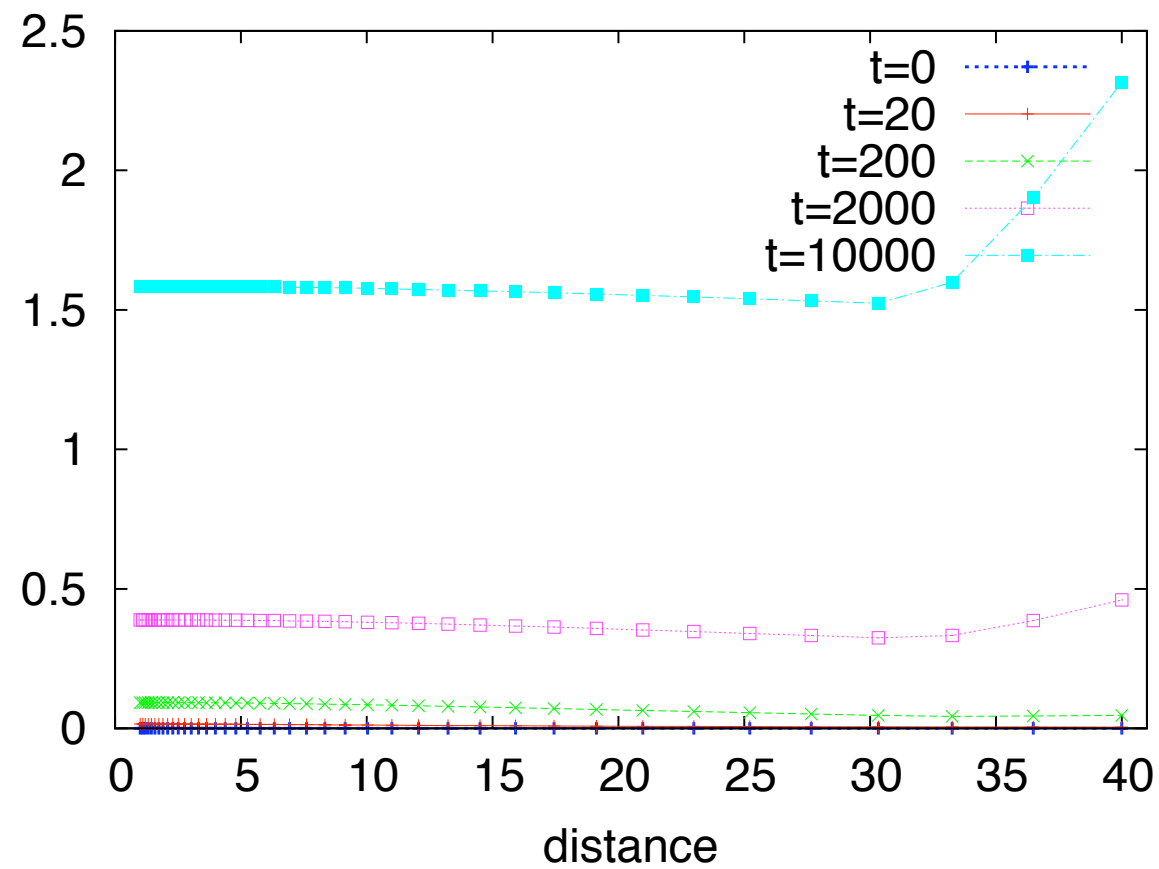
Tilt evolution



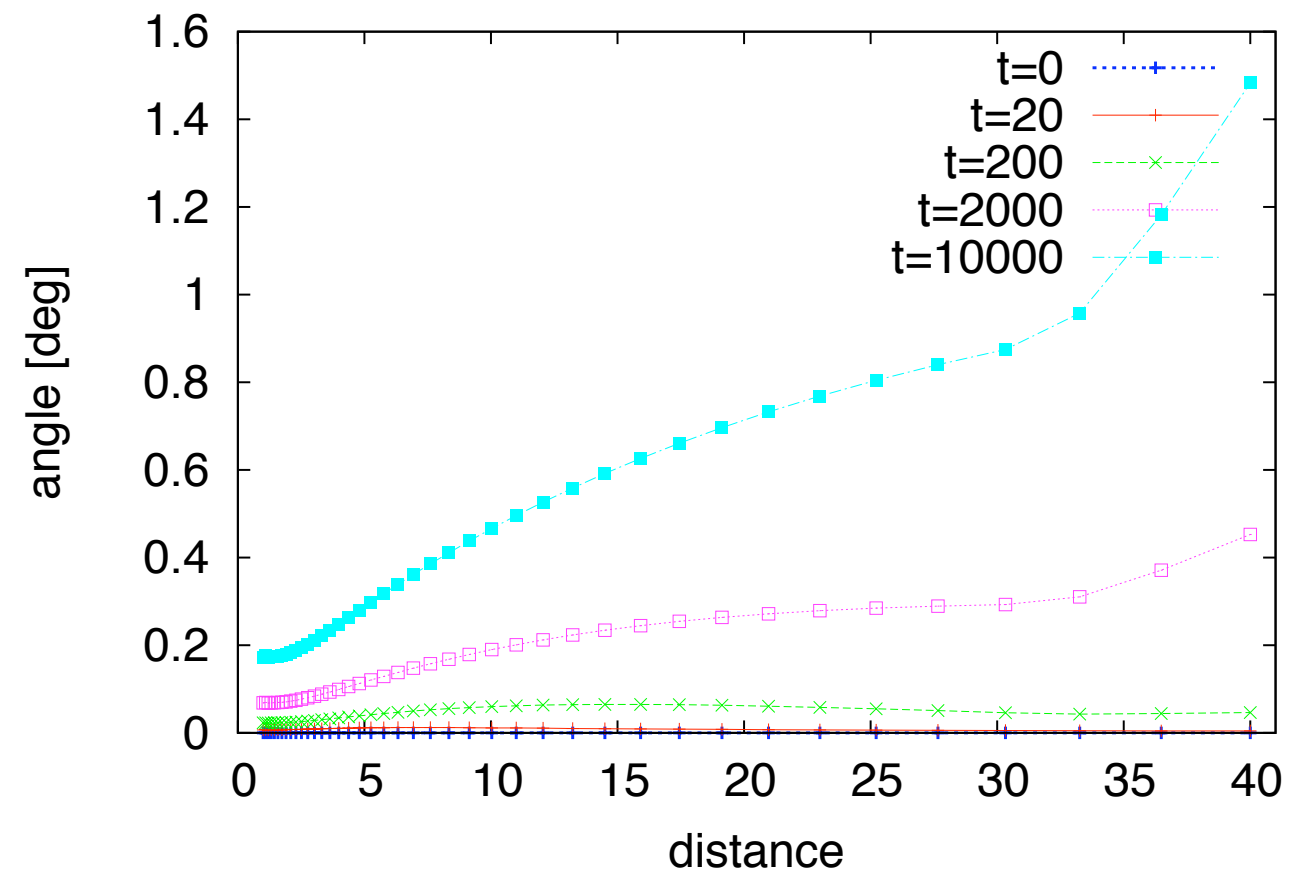


RR toy model

inclination, with RR no BP, initial inclination ~ 0 deg

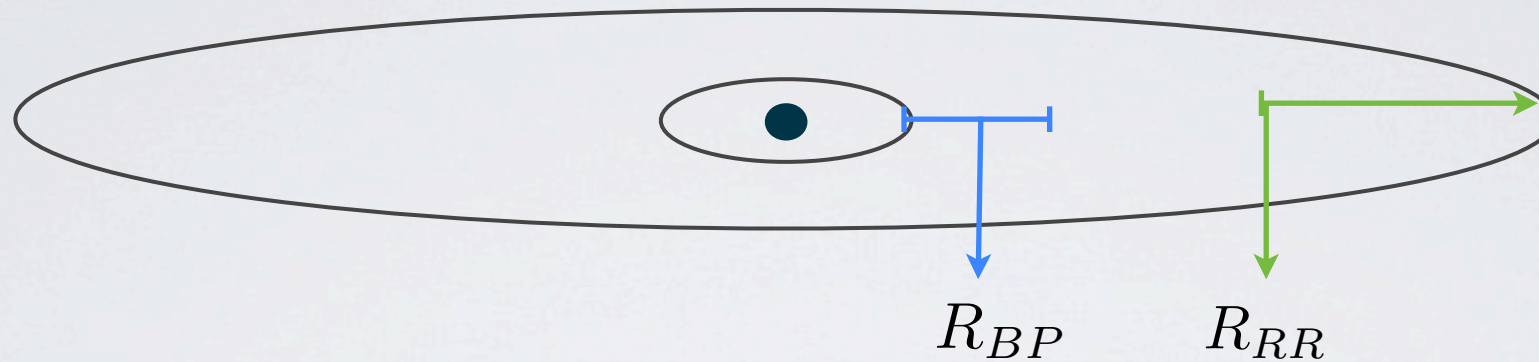


inclination, with RR with BP, initial inclination ~ 0 deg



$$M_{\bullet}/M_{\star} = 1e6 \quad \nu_1 = \nu_2 = 1 \quad \gamma = 1.5$$

torques field



Precession angular velocity

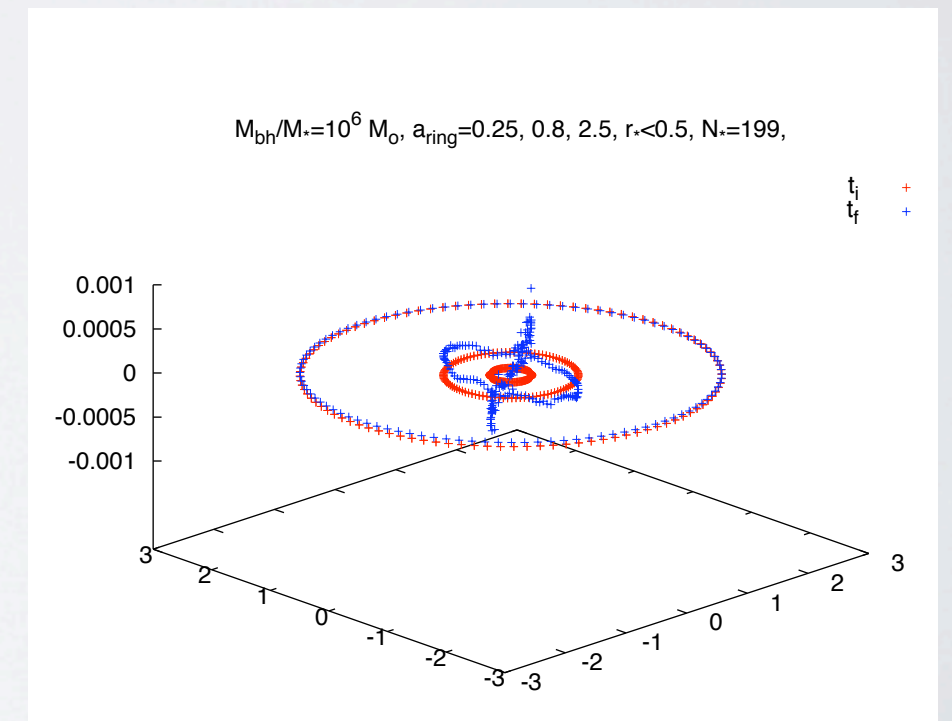
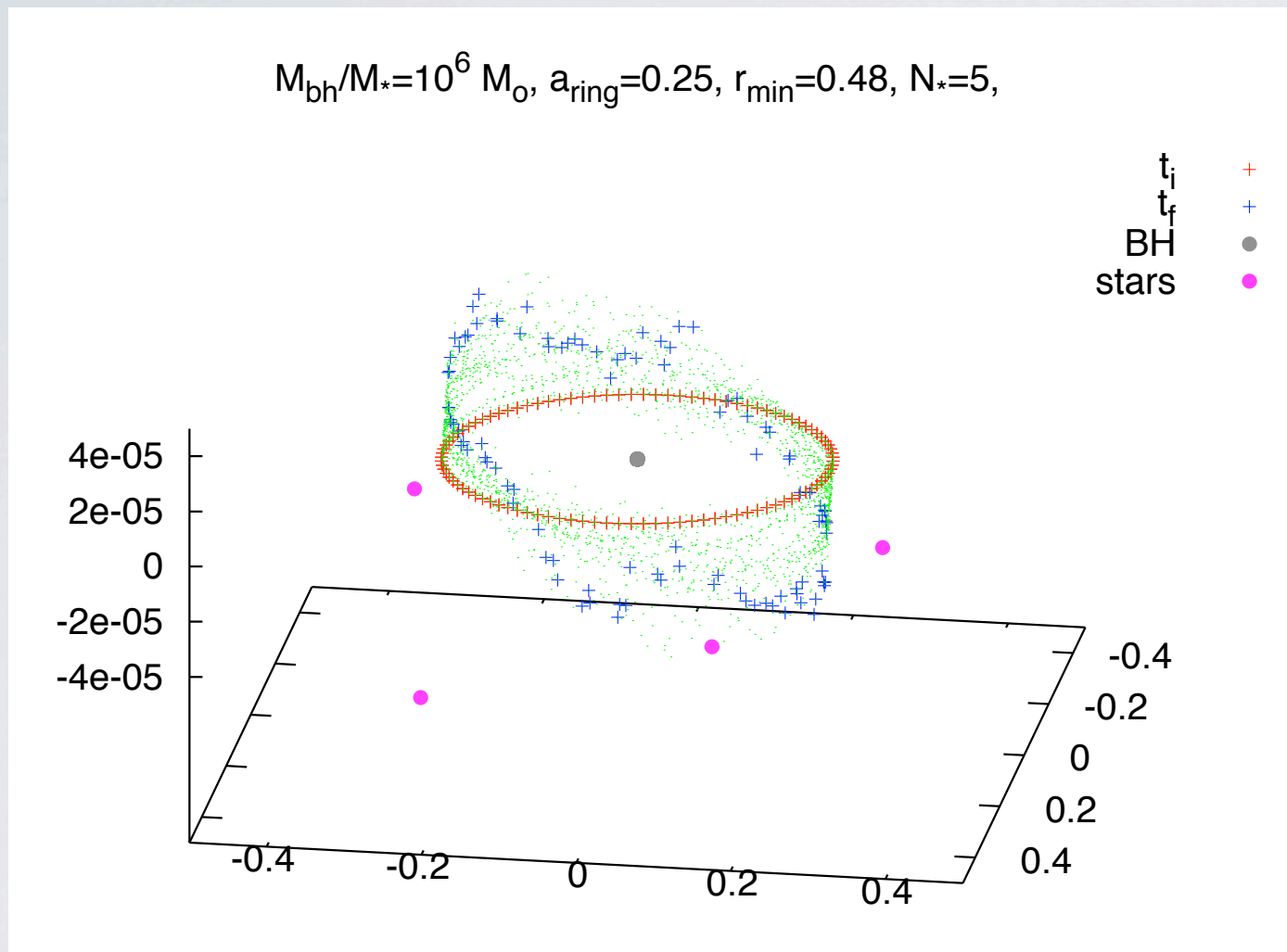
$$\Omega_{LT} = \frac{2G}{c^2} \frac{J_{\bullet}}{r^3} \quad J_{\bullet} = a_* GM_{\bullet}^2 / c$$

$$t_{BP} = R_{BP}^2 / \nu_2$$

$$t_{vRR} = R_{RR}^2 / \nu_2$$

RR torquing redefine the inclination angle of the disc for the BP alignment on t_{RR} time scale

Results - simulations



N-body simulations, using the code developed by G. Kuper (2007)

Open questions

- Are there enough stellar black holes so close to the MBH to affect the disk?
- Will RR completely disrupt the disk?

Summary

- Poisson fluctuations in stellar distribution transfer momentum from stars to maser disk and excite torque.
- RR inherent to discreteness to stellar system: does not require special disk initial conditions.
- RR induced warps are transient, vary on a timescale
 $t_{vRR} \sim \text{few} \times 10^7 \text{ yr}$
- RR warping mechanism dominates warping dynamics faster than other suggested mechanisms. $t_{BP} > \text{few} \times 10^9 \text{ yr}$
- RR may rotate MBH spin vector by the Bardeen - Petterson coupling of the disk's orientation at large radii with the MBH spin direction.